

# BASICS OF NMR/MRI



# Content

## Part 1: Basics of NMR/MRI

- History of MRI
- The NMR phenomena
- Basic MR concepts: magnetization, precession, resonance, excitation, relaxation
- Spatial encoding with imaging gradients



# History of NMR and MRI

- 1923: Wolfgang Pauli describes the phenomena of nuclear spin.
- 1944: Nobel Prize in Physics: Isidor Isaac Rabi “for his resonance method for recording the magnetic properties of atomic nuclei”.
- 1946: The American scientists Felix Bloch and Edward Purcell described, independently, the NMR phenomena.
- 1952: Nobel Prize in Physics: Bloch and Purcell for discovering nuclear magnetic resonance spectroscopy.
- 1972: US Patent 3789832; “Apparatus for detecting Cancer in Tissue”. Damadian, March 17, 1972.
- 2003: Nobel Prize in Physiology or Medicine: Paul Lauterbur and Sir Peter Mansfield “for their discoveries concerning magnetic resonance imaging”.



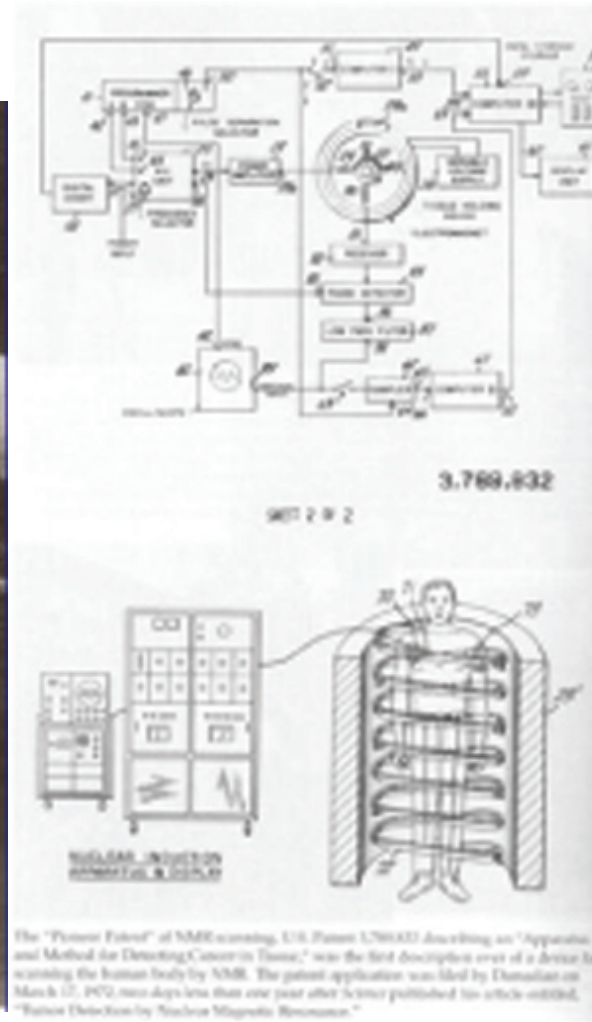
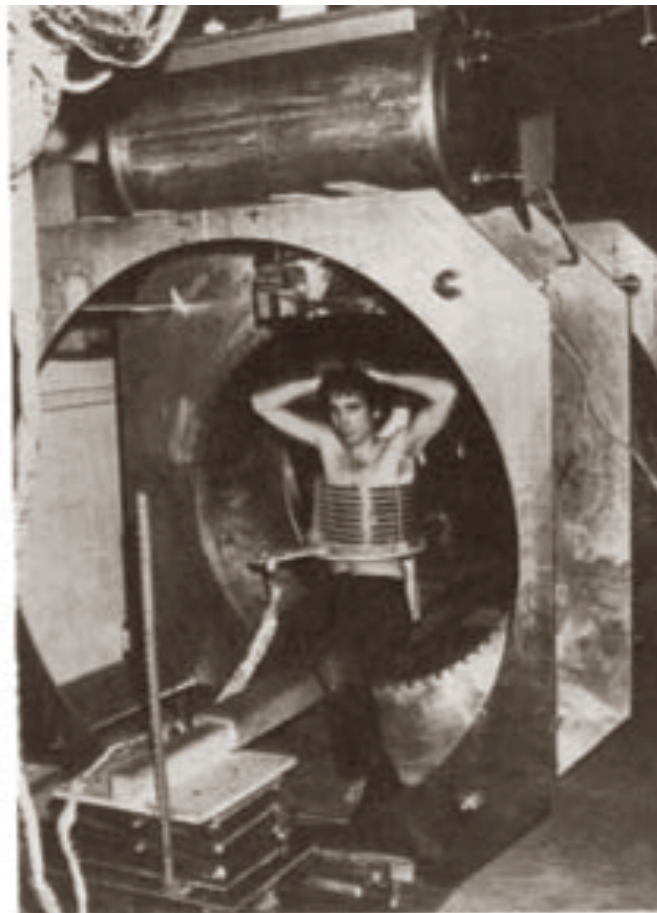
Wolfgang Pauli og Niels Bohr studerer spinn



# History, Cont.

1977: US Patent 3789832; "Apparatus for detecting Cancer in Tissue". Damadian, March 17, 1972.

RIGHT: Although Minkoff was smaller and fit the antenna vest better, he wasn't anxious to risk his health for an experiment that had never been done before. But finally, on July 2, 1977, Minkoff told Damadian that he would go into the machine. That very evening, shortly before midnight, Minkoff took his shirt off and put on the cardboard vest. As soon as the machine was turned on, there was a signal. Four hours and 45 minutes later, after Minkoff had been incrementally moved via the adjustable seat into different positions, the first whole-body human scan showing a cross-section of Minkoff's chest was complete. An ecstatic Damadian noted his jubilant reaction in Goldsmith's notebook (NEXT PAGE).



# History, Cont.

**THIS YEAR'S NOBEL PRIZE  
IN MEDICINE**



## **30 years of proof that this shameful wrong must be righted**

**Why the idea of an MRI didn't occur to this year's two winners until  
after a medical doctor made his landmark discoveries**

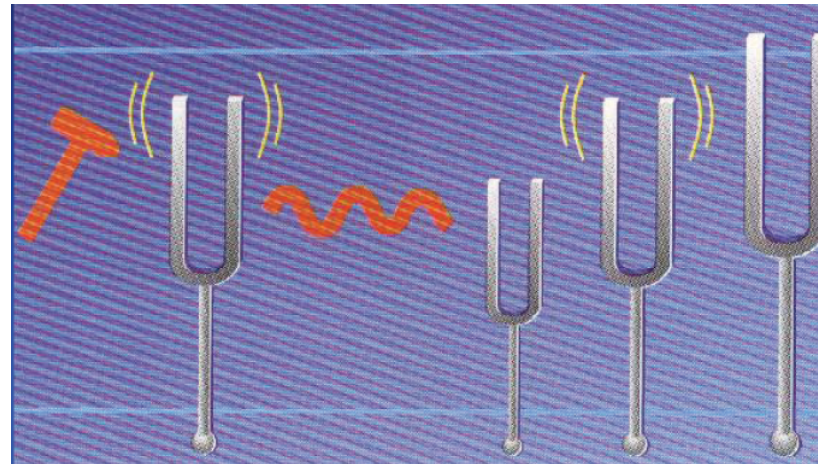
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# The NMR Phenomena

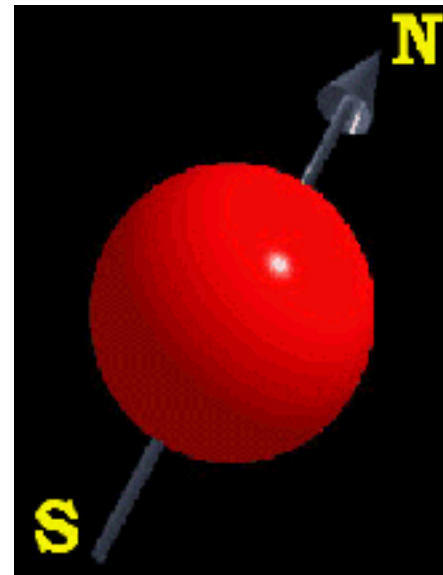
- Bloch and Purcell discovered that if you put protons (or certain **nuclei**) in a powerful **magnetic** field and then send *electromagnetic radiation* onto them, they will produce a *signal* in a *coil* placed around the protons.
- The radiation must have a frequency that the protons can “hear” (i.e., they **resonate**) in order to absorb and then release energy

⇒ **Nuclear Magnetic Resonance or NMR**



# The Source of MR Signal

- MR sensitive nuclei have an uneven number of protons or neutrons in their nucleus.
  - Examples:  $^1\text{H}$ ,  $^3\text{He}$ ,  $^{13}\text{C}$ ,  $^{15}\text{N}$ ,  $^{17}\text{O}$ ,  $^{19}\text{F}$ ,  $^{23}\text{Na}$ ,  $^{31}\text{P}$ ,  $^{129}\text{Xe}$
- Such nuclei have a quantum property called **SPIN**
- Spin is a form of **ANGULAR MOMENTUM**



# Spin/Spins Interacting with a Magnetic Field

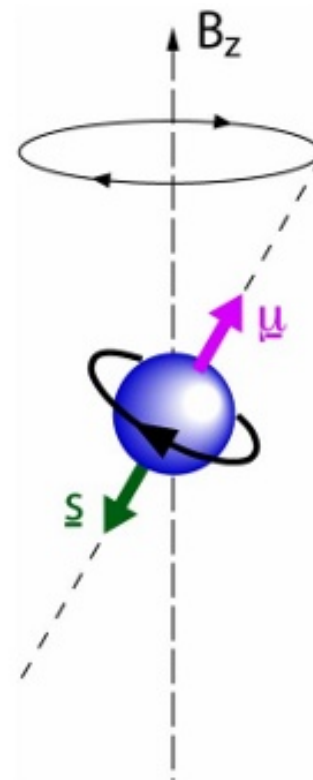
- What happens to a single spin when magnetic field is applied?
  - **RESONANT PRECESSION** around  $B_0$  with a characteristic frequency, which depends on  $B_0$
- What happens to a large number (ensemble) of spins when a magnetic field is applied?
  - **RESONANT PRECESSION** around  $B_0$  with a characteristic frequency
  - Development of a net **MAGNETIZATION**, which also depends on  $B_0$





# Resonant Precession

- Spins **PRECESS** (rotate) in the plane perpendicular to the magnetic field axis.
- This phenomena is described, using purely classical mechanics, as a **GYROSCOPE**



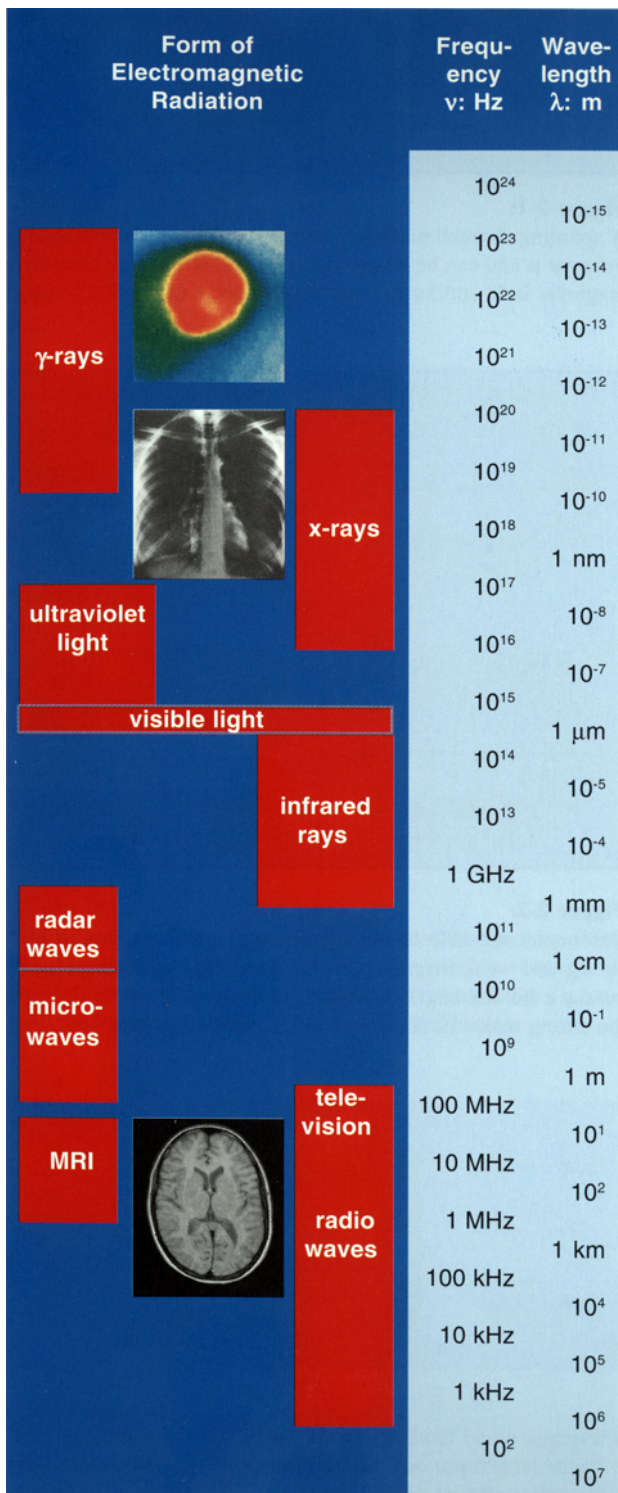
# Resonant Precession, Cont.

- The frequency of precession is called **LARMOR FREQUENCY**
- Larmor frequency depends on the:
  - strength of the magnetic field ( $B_0$  provides the torque for this precession)
  - “magneto-rotational” property of each nuclei (ratio between magnetic moment and angular momentum)

**=> LARMOR EQUATION:  $f_0 = \gamma * B_0$**

- $f_0$  = Resonant frequency (Larmor frequency, precession frequency, in Hz)
- $\gamma$  = Gyromagnetic ratio (constant = 42,58MHz/T for  $^1\text{H}$ )
- $B_0$  = Static magnetic field (7T on “our” MR)
  
- Ex1: Clinical MRI machine uses 1.5T =>  $f_0 = 64 \text{ MHz}$
- Ex2: 7T Pharmascan =>  $f_0 = 300.3\text{MH}$

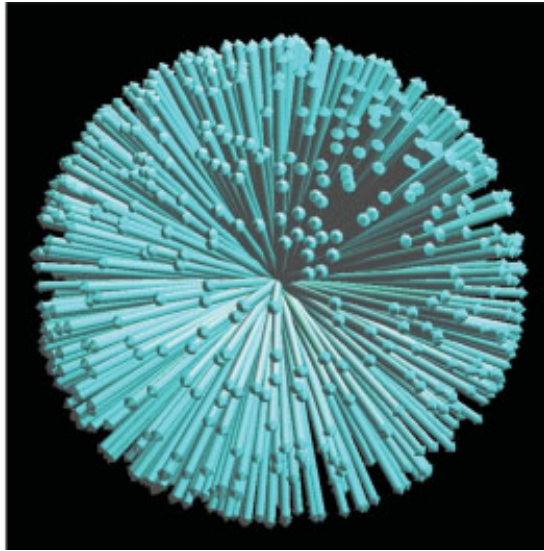




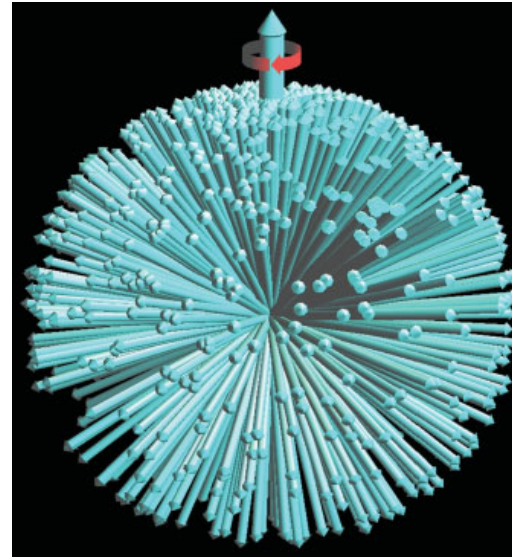
# The magnetic field

- Magnetic field strength is measured in Tesla (T) or Gauss (G)
- One Tesla = 10 000 Gauss.
- We use a 7T MR = 140 000 times stronger than the earth's magnetic field (0.05 mT).

# Magnetization



No magnetic field



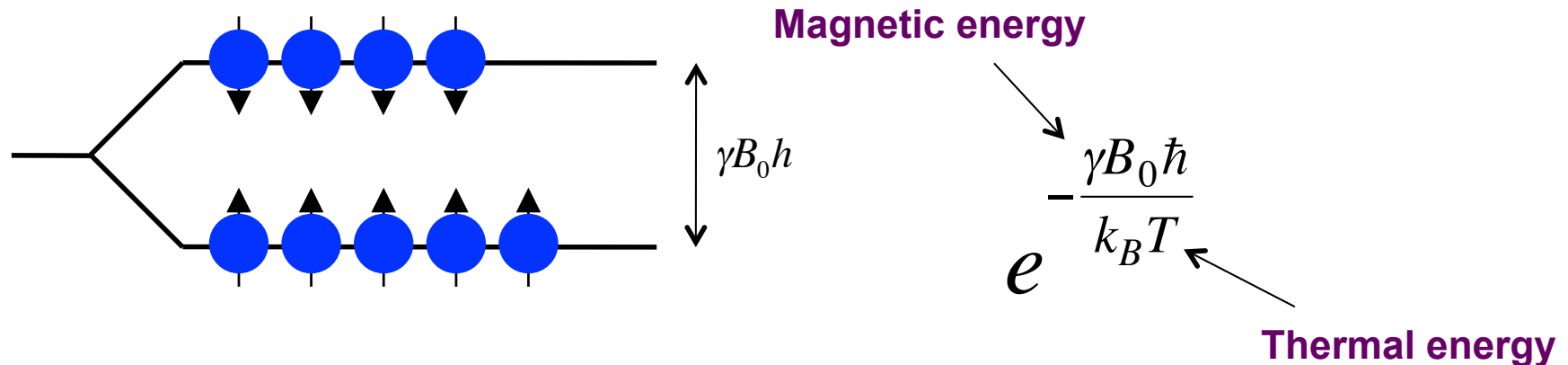
Magnetic field present





- In the absence of mag. field, spin distribution is randomly oriented in all directions.
- In the presence of mag. field, spin distribution is very slightly skewed towards the magnetic north → **MAGNETIZATION**



# Magnetization, an Alternative View



- Spins have two energy eigenstates: spin up  (low energy state) and spin down  (high energy state).
- At room T, thermal energy  $\gg$  magnetic energy, so the access of spins in low energy state vs. high energy state is 1 in 1 mill.
- Body is 2/3 water  $\rightarrow$  lots of protons and thus spins  $\rightarrow$  the excess number of spins in the lower energy state becomes big enough to be detected
- This spin excess is called **MAGNETIZATION**

[Video: Introduction to Nuclear Magnetic Resonance](#)



# Excitation

- From now on we will only be describing the behavior of net magnetization  $M$  (i.e., ignore the behavior of individual spins).
- **$M$  is the source of MR signal and is used to produce MR images**
- In equilibrium,  $M$  is aligned with  $B_0 \rightarrow$  no precession around  $B_0 \rightarrow$  no emission of EM radiation.
- To produce an MR signal,  $M$  has to be tipped away from the  $B_0$  field.
- This is achieved with an **RF pulse** which is produced by an **RF coil** whose long axis is oriented perpendicular to the direction of  $B_0$  field.
- RF pulse tips  $M$  away from  $B_0 \rightarrow M$  precesses around  $B_0 \rightarrow$  emission of RF radiation  $\rightarrow$  detection of RF radiation by the RF coil via Faraday's law of induction (can be the same coil as the one that excited  $M$ ).

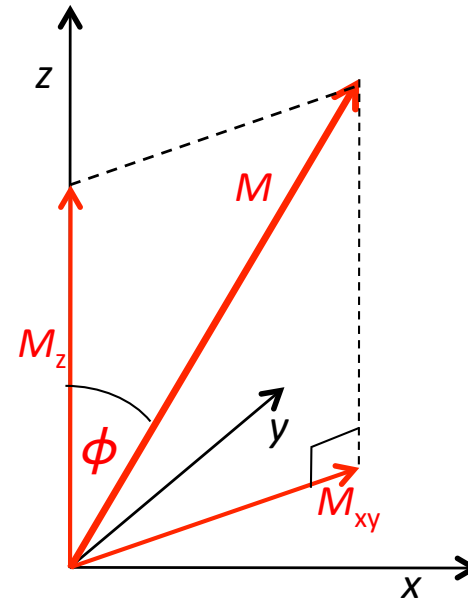


## Excitation, Cont.

$$\omega_0 = \gamma B_0 \text{ and } \omega_1 = \gamma B_1$$

$$\Rightarrow \frac{d\phi}{dt} = \gamma B_1$$

$$\Rightarrow \Delta\phi = \gamma B_1 \Delta t$$



- Flip angle by which  $M$  is tipped away from  $B_0$  is proportional to the strength and the length of the  $B_1$  pulse.
- A  $\pi/2$  RF pulse flips  $M$  by a  $90^\circ$  angle, a  $\pi$  RF pulse flips  $M$  by  $180^\circ$ .
- $M$  has now 2 vector components: a longitudinal component,  $M_z$ , which is parallel to  $B_0$ , and a transverse component,  $M_{xy}$ , which is perpendicular to  $B_0$ .
- Signal that is detected by the RF coil is called an FID (**FREE INDUCTION DECAY**).
- FID is precession of  $M_{xy}$  (transverse component) around  $z$ -axis.



# Video 1: Precession, Resonance and Excitation

**Introductory NMR and MRI  
with Paul Callaghan**

Video 1  
Precession and Resonance





# Relaxation

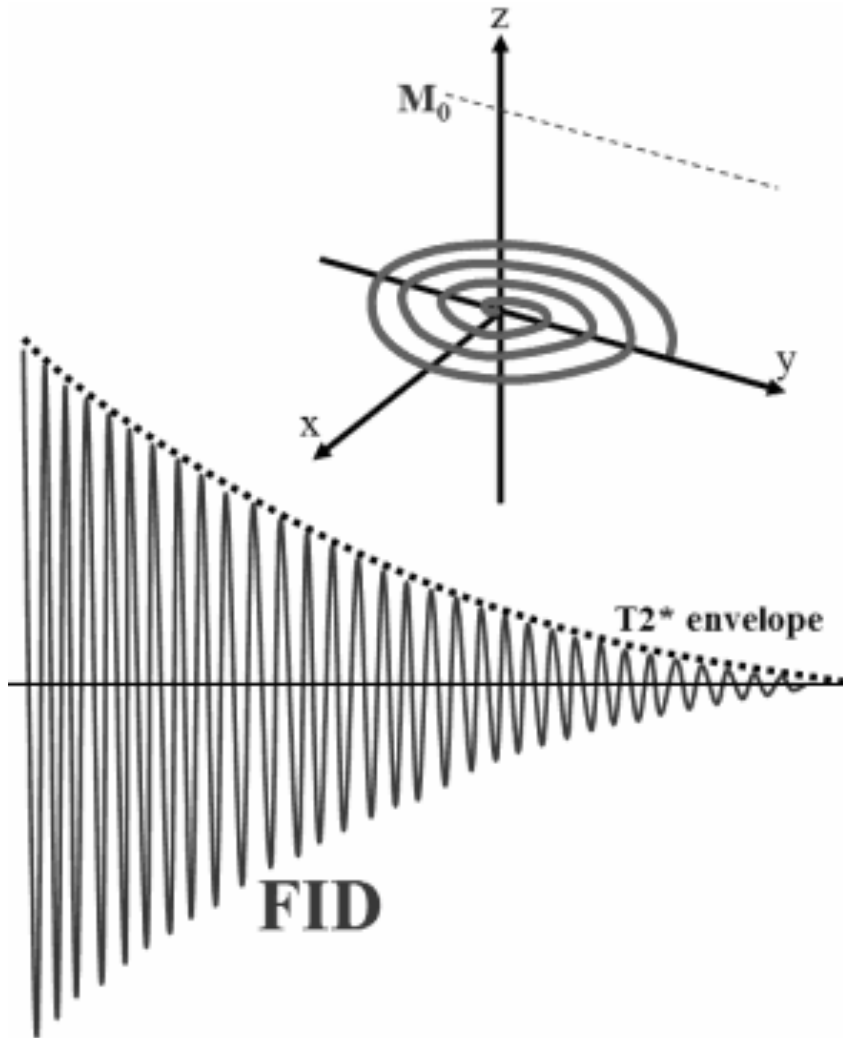


# Relaxation

- After RF pulse tips  $M$  away from  $B_0$  and is turned off, magnetization relaxes back to its equilibrium state.
- Two main **RELAXATION** processes present:
  - $T_2$  **relaxation** or  $T_2$  decay
  - $T_1$  **relaxation** or  $T_1$  recovery
- These processes occur simultaneously. However:
  - In liquids,  $T_1 \approx T_2$
  - In solids,  $T_1 \gg T_2$



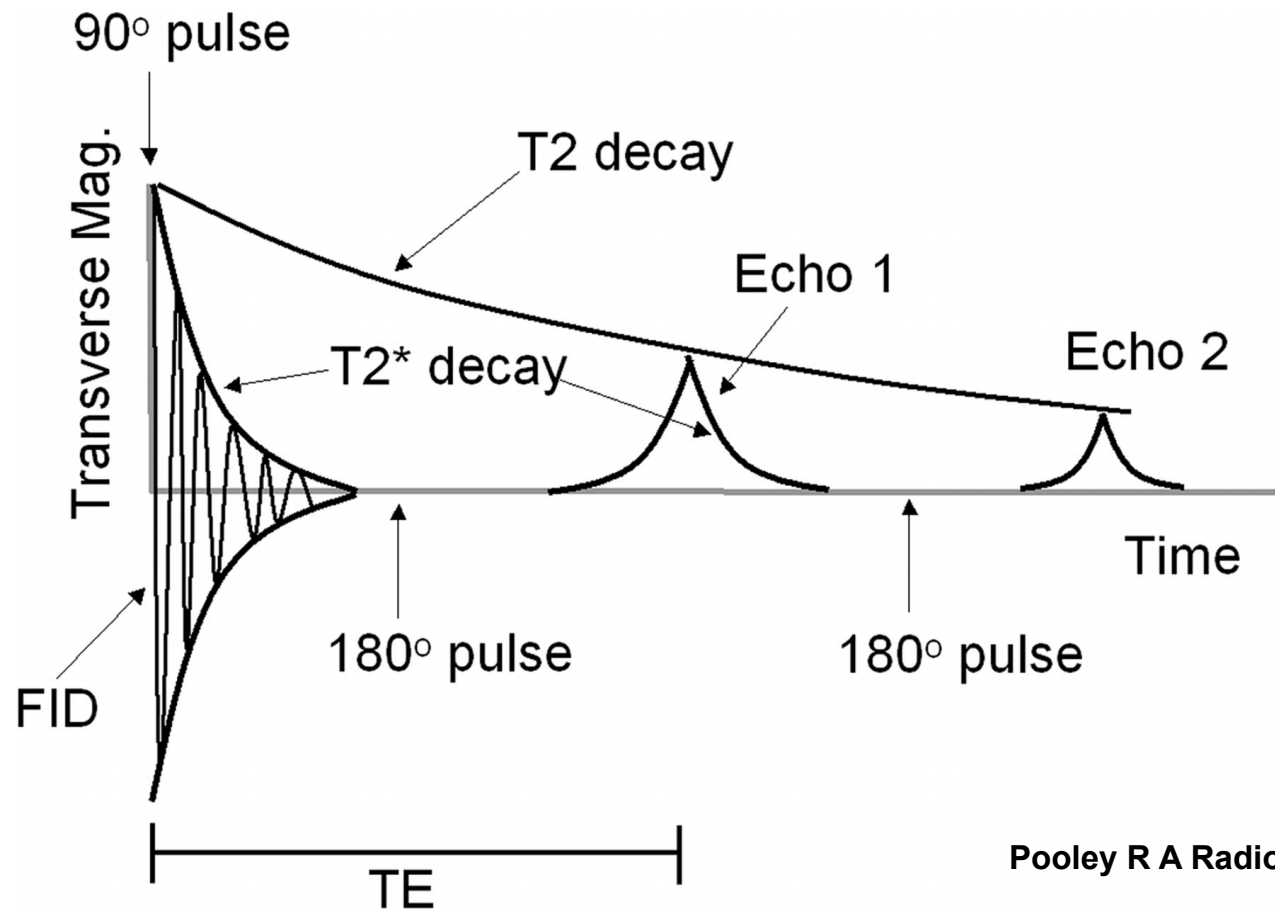
# $T_2$ and $T_2^*$ Relaxation: Free Induction Decay



- After the RF pulse,  $M_{xy}$  decays due to:
  - SPIN-SPIN INTERACTIONS which cause de-phasing or loss of phase coherence  $\rightarrow$  unrecoverable loss
  - STATIC MAGNETIC FIELD INHOMOGENEITIES present over the sample  $\rightarrow$  recoverable loss
  - MAGNETIC SUSCEPTIBILITIES  $\rightarrow$  recoverable loss
- $T_2^*$  relaxation is due to all causes above
- $T_2$  relaxation is due to spin-spin relaxation (property of the spin system)



# $T_2$ and $T_2^*$ Relaxation: Spin-Echo Train

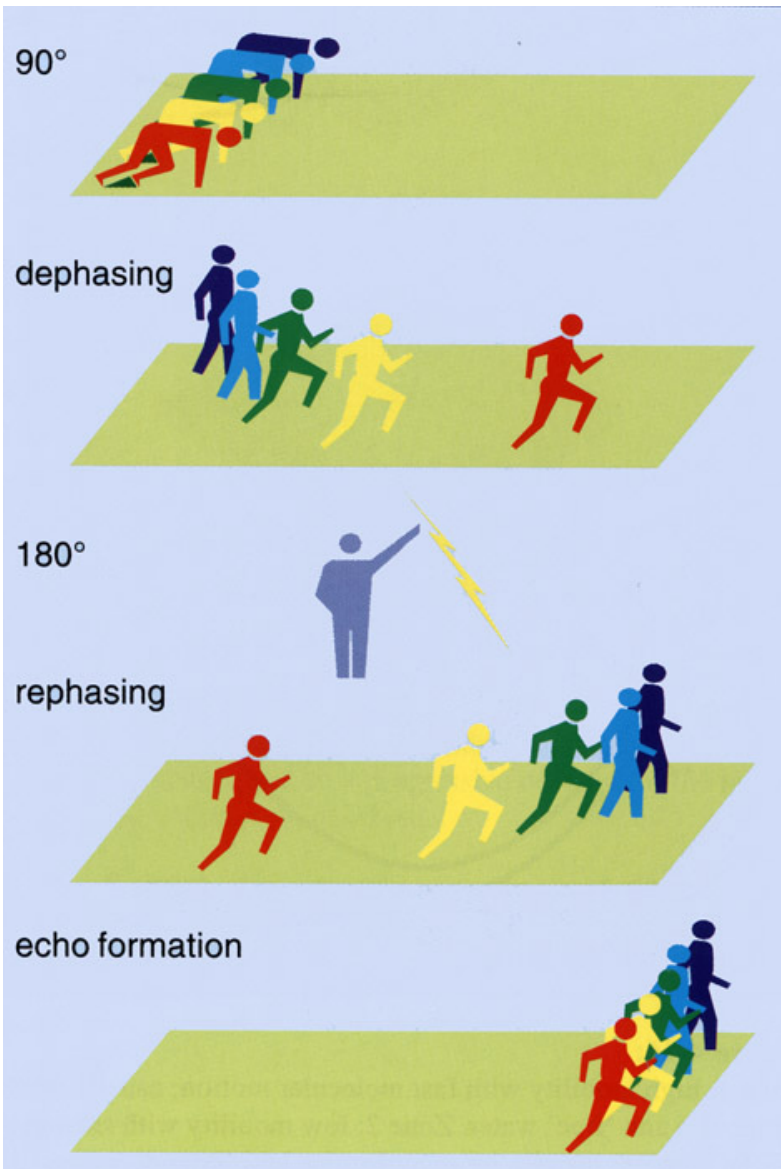


Pooley R A Radiographics 2005;25:1087-1099

- Spin-echo envelope decays with  $T_2$  RELAXATION time constant
- The width of each echo is related to  $T_2^*$  RELAXATION time constant



# A Cartoon View of Spin Echoes



At the time of the  $90^{\circ}$  pulse, the runners are lined up at the starting line.

After the  $90^{\circ}$  pulse, the fast runners separate from the slow runners.

At a certain time during the race, the runners are transposed.

Now the fast runners are behind the slow ones, but they catch up.

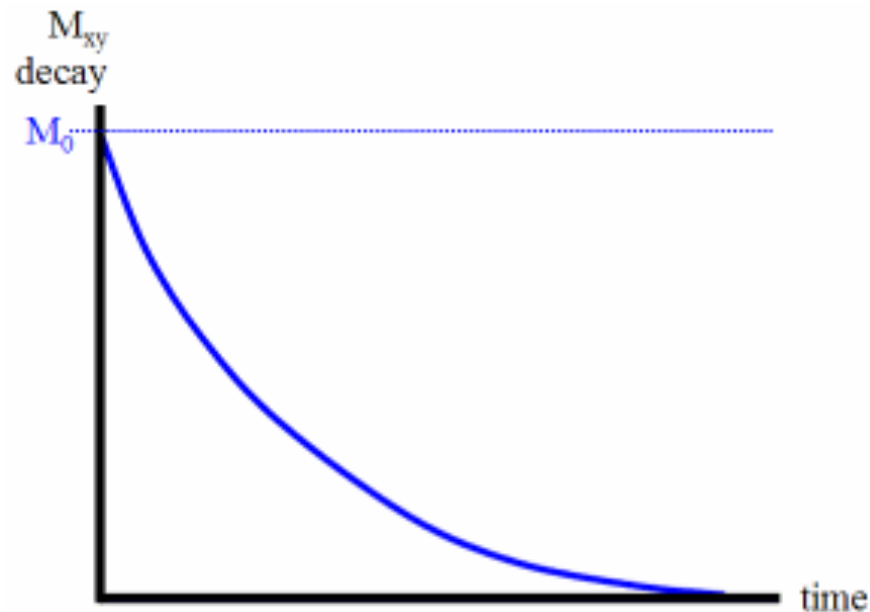


# $T_2$ Relaxation: Mathematical Description

$$\frac{dM_{xy}}{dt} = -\frac{M_{xy}}{T_2}$$

After a  $90^\circ$  pulse,  $M_{xy}(0) = M_0$

$$M_{xy} = M_0 e^{-t/T_2}$$

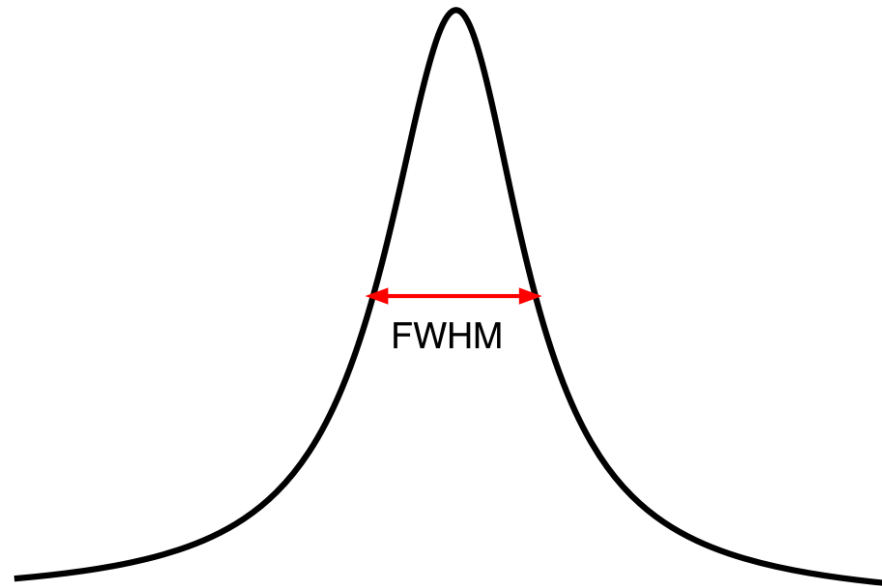


# $T_2^*$ Relaxation: Mathematical Description

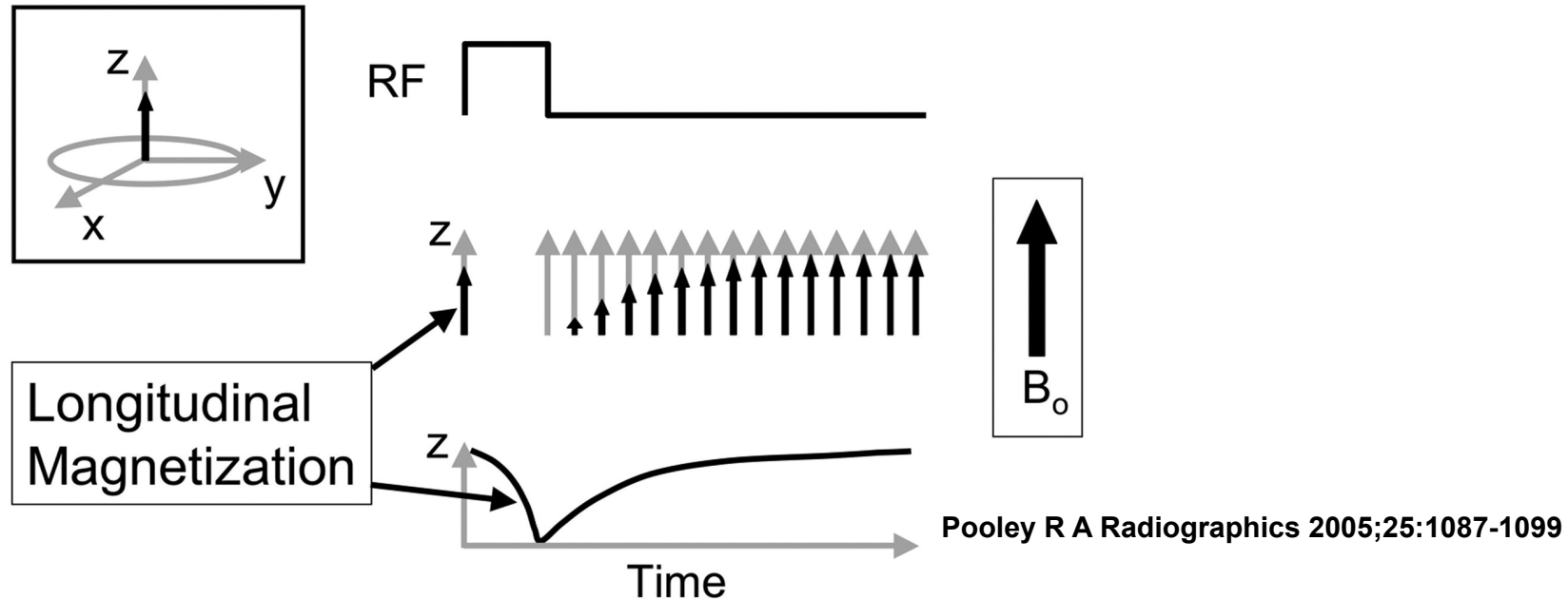
$$\frac{1}{T_2^*} = \frac{1}{T_2} + \frac{\gamma}{2\pi} \Delta B$$

- $T_2^*$  is related to the width of the FT (Fourier Transform) of FID

$$FWHM = \frac{1}{\pi T_2^*}$$



# $T_1$ Relaxation: Recovery of $M_z$



- After the RF pulse,  $M_z$  grows back to its equilibrium along z-axis
- This process is due to small field fluctuations resulting from moving spins
- The process is independent of  $T_2$  relaxation



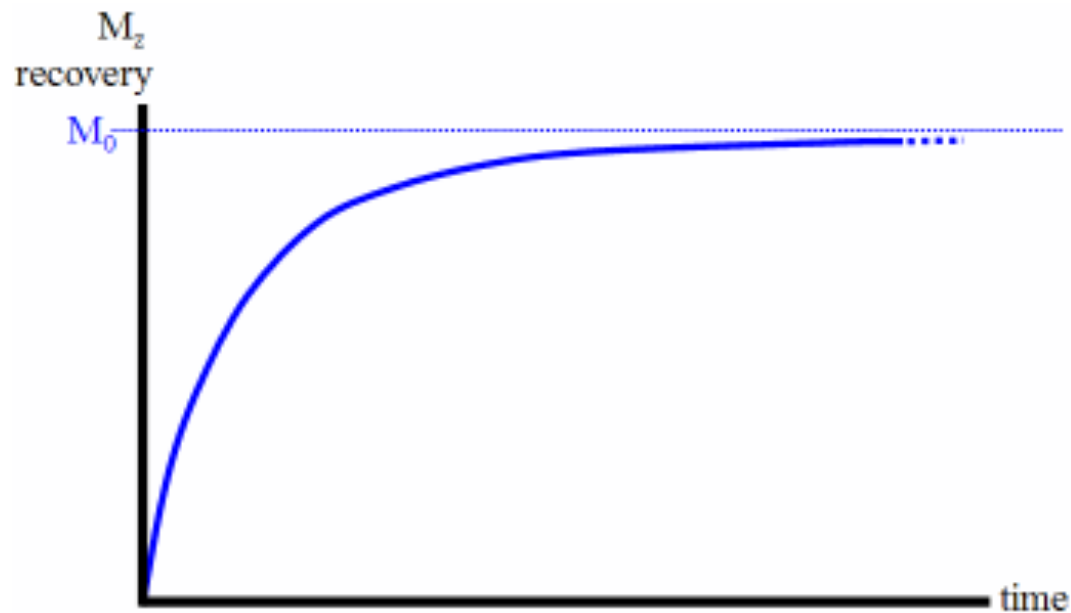


# $T_1$ Relaxation: Mathematical Description

$$\frac{dM_z}{dt} = -\frac{M_z - M_0}{T_1}$$

After a  $90^\circ$  pulse,  $M_z(0) = 0$

$$M_z = M_0(1 - e^{-t/T_1})$$

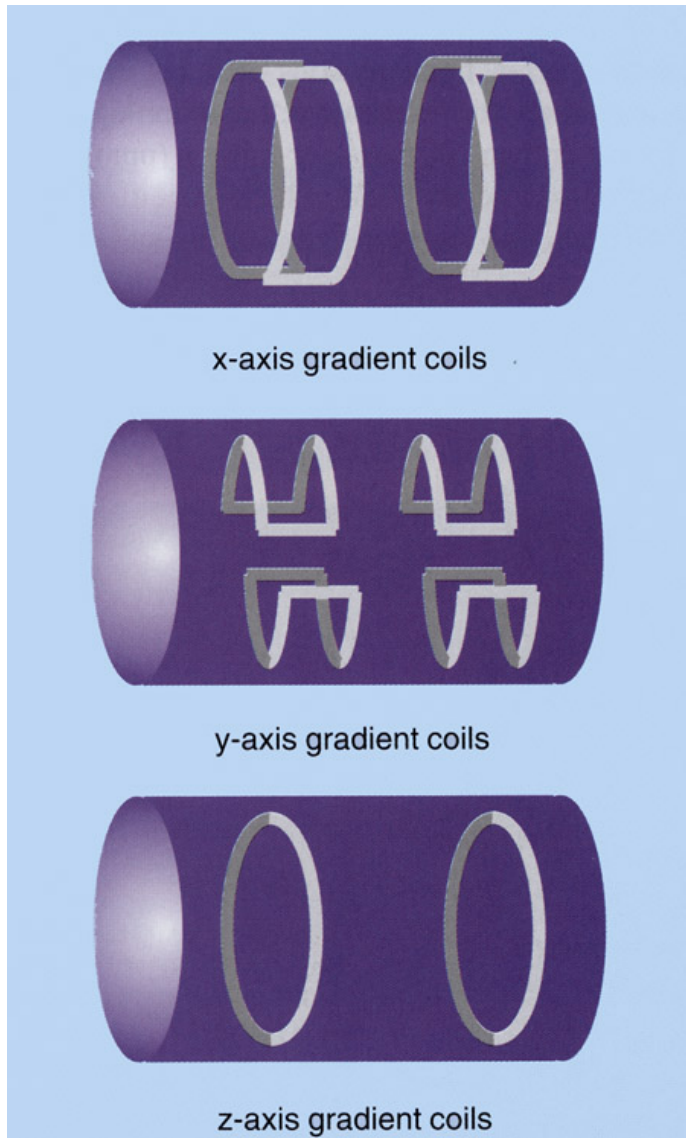


# But, which spins exactly do we image in MRI?

- Generally, in MRI, we detect the resonant precession of protons in Hydrogen ( $^1\text{H}$ ).
- The Hydrogen atom is a component of water and fat →  
We image both water and fat (unless we suppress signal from fat)
- Body consists of 2/3 water → a lot of spins → large magnetization → large potential signal
- An RF coil placed near the body will detect the precession of this magnetization, however, this will be a net signal from the entire body (or coil sensitive region)
- **QUESTION: how do we distinguish signals from different parts of the body?**



# Imaging Gradients

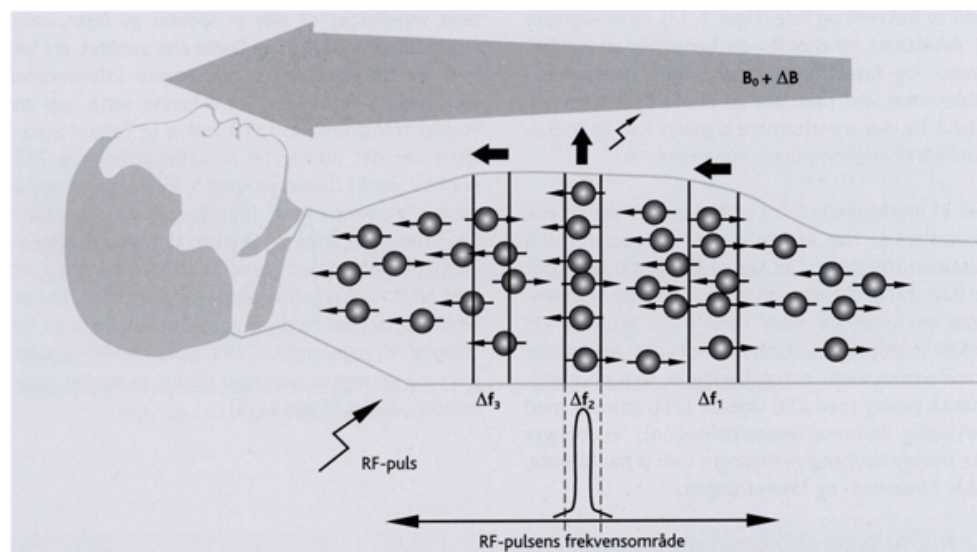


- There are coils which produce the main magnetic field ( $B_0 = 7\text{T}$  in our case).
- In addition, there are several other coils making small, additional magnetic fields which vary linearly in space. These are called **gradient coils**.
- These small additional magnetic fields are present in X, Y and Z direction. Without them, we can not say where in the tissue the signals come from.



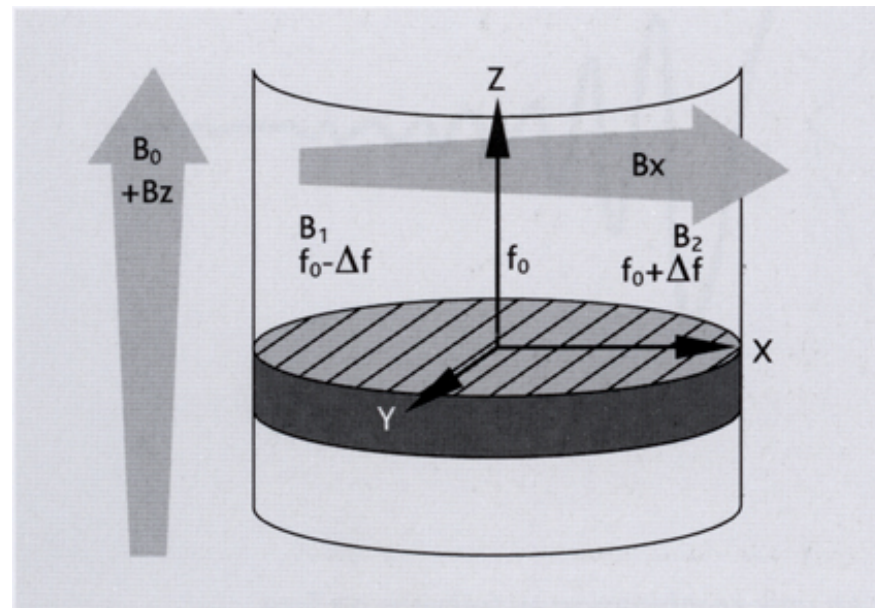
# Slice Selection

- Slice selective gradients,  $G_z$ , are put "on top" of the static magnetic field, in order to change the Larmor frequency along slice direction  $\Rightarrow f(z)$ .
- A specially designed RF excitation pulse is applied at the same time as the gradient. This RF pulse contains a narrow range of RF frequencies, centered about the Larmor frequency.
- RF only excites the spins which are on-resonance with the RF pulse  $\Rightarrow$  **SLICE SELECTION**.
- You cut salami into small slices!



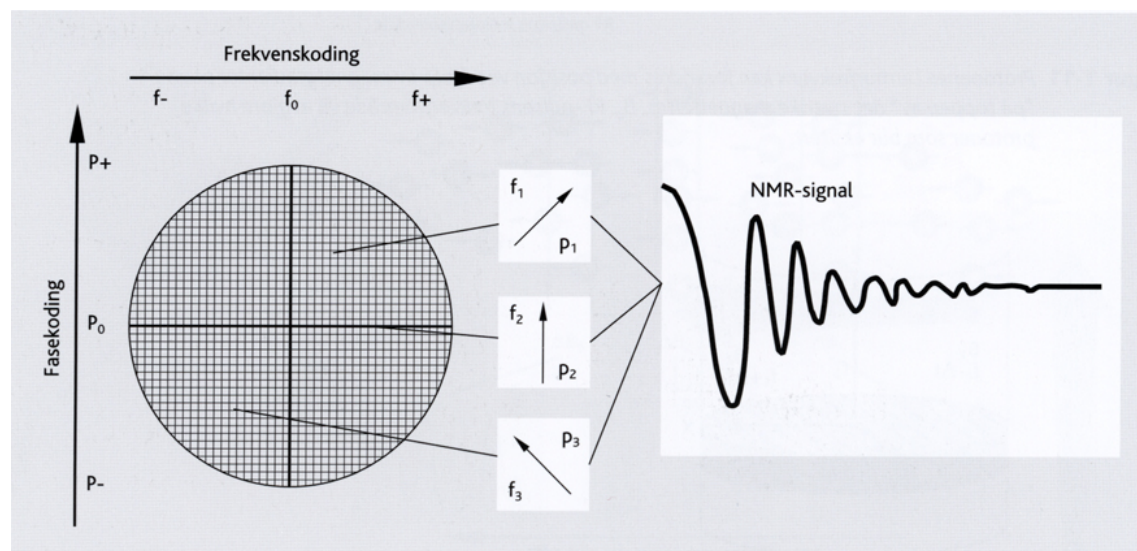
# Frequency Encoding

- A constant gradient (usually along x-axis),  $G_{FE}$  or  $G_{read}$ , is applied continuously during readout of the MR signal.
- Signals which are sampled at different time-points during the readout will have different spatial frequency => **FREQUENCY ENCODING**
- Applying FT (Fourier Transform) along this direction will produce a 1D projection of the object
- You cut the salami slice into thin strips!



# Phase Encoding

- A gradient (usually along  $y$ -axis),  $G_{PE}$ , is applied for a certain period of time after RF excitation and before signal readout/detection.
- Spins will dephase (acquire phase difference in relation to each other) depending on the position along the gradient. This happens because the  $Y$  gradient gives different spins different Larmor frequency.
- When the gradient is turned off, the frequency will go back to the original value, but the phase difference will be kept => **PHASE ENCODING**.
- This process has to be repeated for many different  $G_{PE}$  values in order to sample the entire range of spatial frequencies



# Gradient Summary

- Z direction: Slice selection. Gradient ON at the same time as the RF excitation.
- X direction: Frequency encoding. Gradient ON at the same time as the readout.
- Y direction: Phase encoding. Gradient ON for a specific duration before readout.



# Video 2: Introduction to k-space

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## Introductory NMR and MRI with Paul Callaghan

Video 9  
Part I: Introduction to k-space





# System components

- A powerful magnet: 7T(ours) or 1.5-3T (clinical)
  - The magnet is supraconductive: IT IS ALWAYS ON
- Gradient coils
- Radio transmitter and radio receiver
- Powerful computer to reconstruct images
- A storage utility (images take space)



# Section Summary

- Spin angular momentum
- Resonant precession and Larmor frequency
- Magnetization
- Excitation
- Relaxation
- Imaging gradients
- Hardware

