

## CONTRAST (CNR) IN MRI



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### Computing CNR

- CNR (contrast-to-noise ratio) is a measure of how distinguishable two structures are from each other.
- For magnitude images (most commonly used in MRI), the contrast-to-noise ratio is:

$$CNR = SNR_1 - SNR_2 = \frac{0.655 \cdot (S_1 - S_2)}{\sigma_{air}}$$

- This relationship tells us that:
  - High SNR does not mean high CNR
  - High CNR necessitates regions with high and regions with low SNR (i.e., bright and dark regions)



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## Factors Influencing CNR in MRI

- Physical and instrumental parameters
  - Magnetic field strength (through  $T_1$  field dependence)
  - Contrast agents (through  $T_1$  dependence)
  - Proton density
  - $T_1$  and  $T_2$  relaxation times of protons in tissue
  - Diffusion coefficient of water in tissue (microstructure environment)
- Imaging sequence parameters
  - Repetition time,  $TR$
  - Echo time,  $TE$
  - Flip angle,  $\alpha$
  - Inversion time,  $TI$
  - Etc (diffusion time, flow parameters, etc...)



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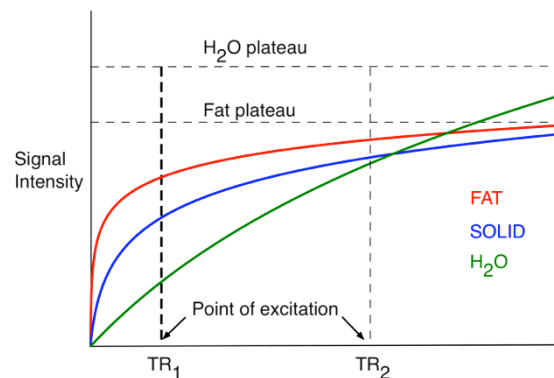
## CNR: $T_1$ and Repetition Time

$$S_{MRI} = \iiint M_0(x, y, z) e^{-i\omega_0 t} e^{-TE/T_2} (1 - e^{-TR/T_1}) f(G(t)) dx dy dz$$

**TR (relaxation time)** is time between each excitation

$T_1$  differs among tissue types, depending on the efficiency of energy transfer:

- $H_2O$ , liquids have long  $T_1$
- Fats have short  $T_1$
- Solids have intermediate  $T_1$



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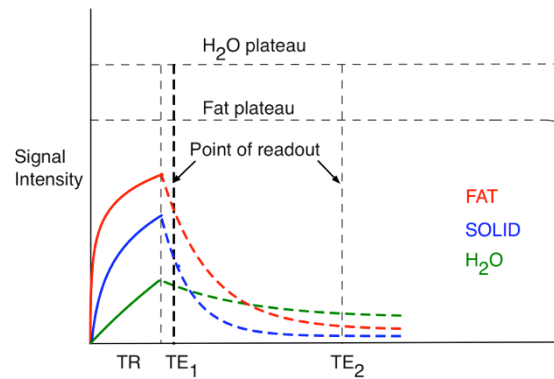
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## CNR: $T_1$ - Weighted Images

- $T_1$ -weighted images produce contrast based on differences in  $T_1$ -relaxation times of tissues
- For  $T_1$  contrast ( $T_1$ -weighting), we need:
  - **Short TR** times to enhance  $T_1$  weighting
  - **Short TE** times to minimize  $T_2$  weighting

$$S_{MRI} \propto \rho_0 (1 - e^{-TR/T_1})$$



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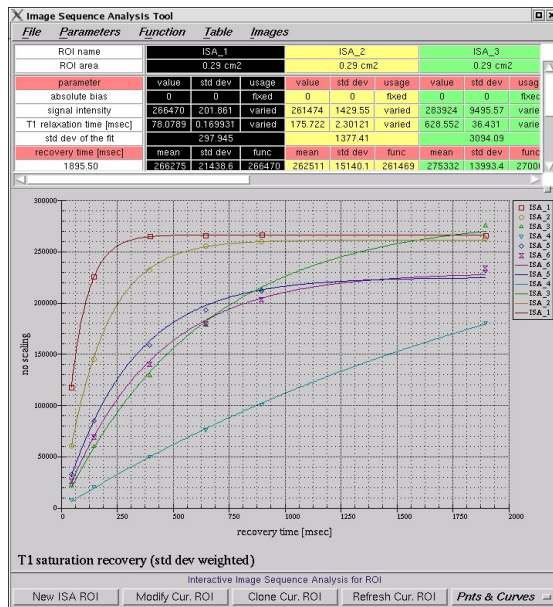
## CNR: $T_1$ - Weighted Images

- **Demonstration:**

- Collect an image of the contrast phantom:
  - Use spin-echo sequence with short TR (200 ms) and short TE (11 ms)
- Observe contrast between different samples
- Explain



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Phantom = 6 tubes:

1. Doped water,  $T_1 \approx 100$  ms
2. Doped water,  $T_1 \approx 200$  ms
3. Doped water,  $T_1 \approx 500$  ms
4. water,  $T_1 \approx 3000$  ms
5. Cooking oil
6. Motor oil



TR=200 ms, TE=11 ms



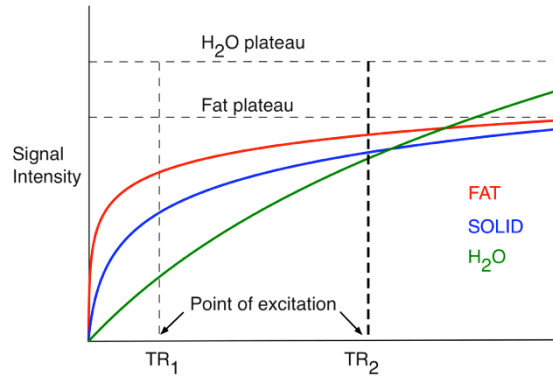
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### CNR: $T_2$ and Echo Time

$$S_{MRI} = \iiint M_0(x,y,z) e^{-i\omega_0 t} e^{-TE/T_2} (1 - e^{-TR/T_1}) f(G(t)) dx dy dz$$

**TE (echo delay time)** is time between between excitation and readout of the signal

- $T_2$  differs among tissue types, depending largely on the mobility of spins:
- H<sub>2</sub>O, liquids have long  $T_2$
  - Fats have intermediate  $T_2$
  - Solids have short  $T_2$



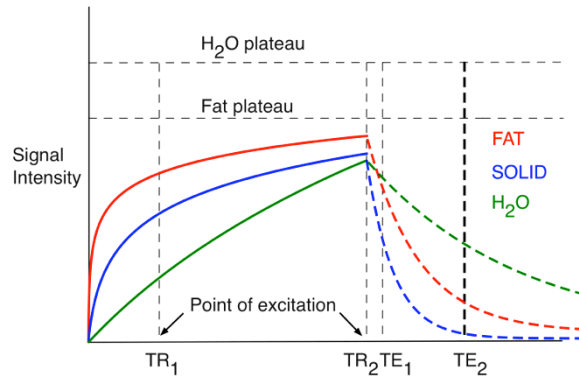
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  - Solids have short  $T_2$



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## CNR: $T_2$ - Weighted Images

- $T_2$ -weighted images produce contrast based on differences in  $T_2$ -relaxation times of tissues
- For  $T_2$  contrast ( $T_2$ -weighting), we need:
  - Long TR times to minimize  $T_1$  weighting
  - Long TE times to enhance  $T_2$  weighting

$$S_{MRI} \propto \rho_0 e^{-TE/T_2}$$



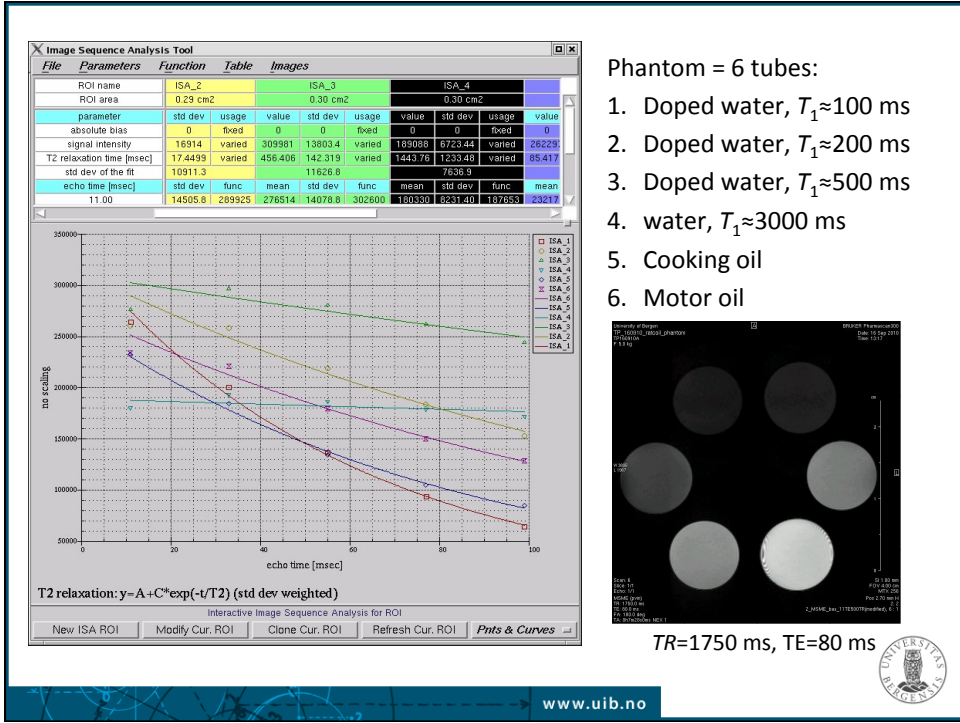
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## CNR: $T_2$ - Weighted Images

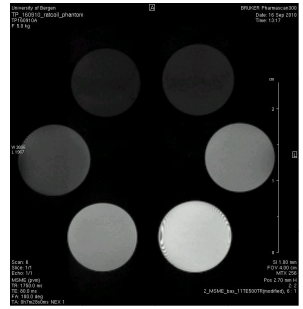
- **Demonstration:**
  - Collect an image of the contrast phantom:
    - Use spin-echo sequence with long TR (1750 ms) and long TE (80 ms)
  - Observe contrast between different samples
  - Explain



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- Phantom = 6 tubes:
1. Doped water,  $T_1 \approx 100$  ms
  2. Doped water,  $T_1 \approx 200$  ms
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  5. Cooking oil
  6. Motor oil



TR=1750 ms, TE=80 ms



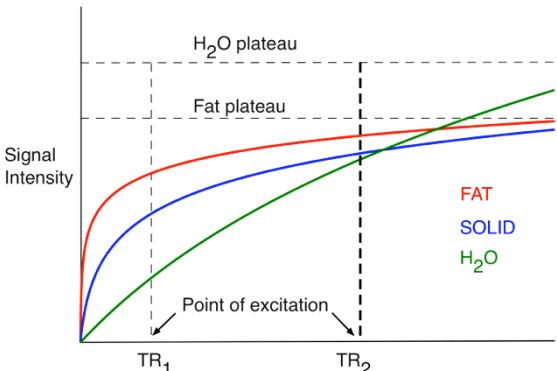
**CNR: Proton Density**

$$S_{MRI} = \iiint \frac{\rho_0 \gamma^2 \hbar^2}{4kT} B_0(x,y,z) e^{-i\omega_0 t} e^{-TE/T_2} (1 - e^{-TR/T_1}) f(G(t)) dx dy dz$$

PD depends on the number of hydrogen atoms (or water content) in tissues

PD varies slightly for different tissue types (muscle, fat, cerebral spinal fluid, gray/white matter, etc):

- Fluids have the highest PD (over 95%)
- Water and fat-based tissues have similar PD (between 60% to 85%)



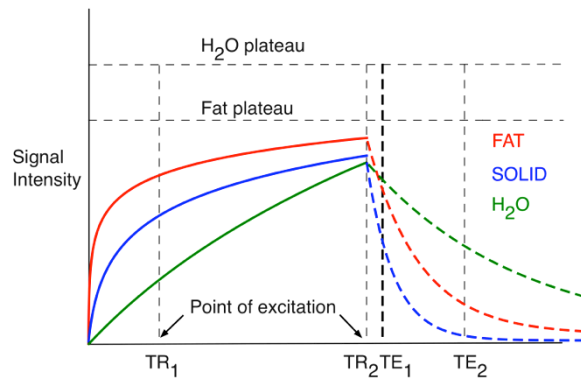
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## CNR: PD- Weighted Images

- PD-weighted images produce contrast based on differences in PD of tissues
- For PD contrast (PD-weighting), we need:
  - **Long TR** times to allow for complete recovery of magnetization (even for longest  $T_1$  components) and minimize  $T_1$  weighting
  - **Short TE** times to minimize  $T_2$  weighting

$$S_{MRI} \propto \rho_0$$

- Note, that pure PD contrast is not achievable in practice, since we would need:
  - Infinitely long TR times
  - TE times equal to 0
- Proton density weighting = We put less *weight* on  $T_1$  and  $T_2$  by lengthening TR and shortening TE, thus giving more *weight* to proton density

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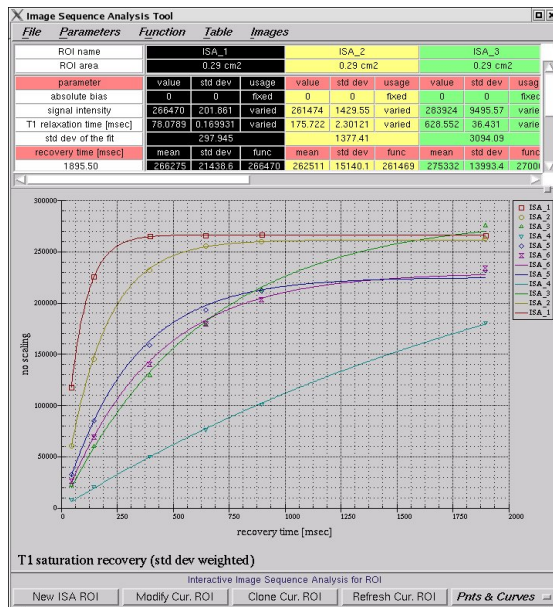
## CNR: PD- Weighted Images

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- Collect an image of the contrast phantom:
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- Observe contrast between different samples
- Explain

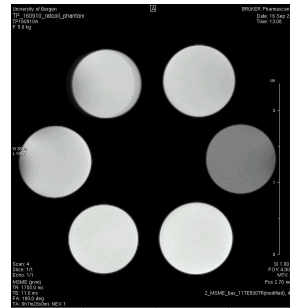


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Phantom = 6 tubes:

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TR=1750 ms, TE=11 ms

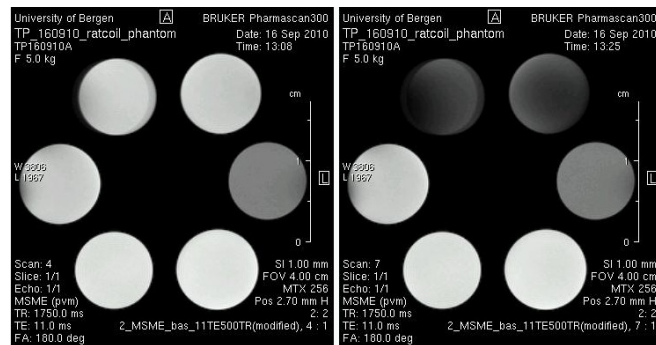


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## CNR: PD- Weighted Images with Fat-Suppression

- **Demonstration:**

- Collect an image of the contrast phantom using fat suppression:
  - Use spin-echo sequence with long TR and short TE
- Observe contrast between different samples
- Explain



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## CNR: Flip Angle

- Flip angle determines contrast in gradient-echo sequence when TR is much shorter than  $T_1$  (FLASH).
- See slide on FLASH for more details

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## CNR: Contrast Agents

- Contrast agents alter relaxation times of water/tissue => **enhance contrast** in the MR images
- Three main types of exogenous contrast agents:
  - Gadolinium, Gd (Omniscan, Magnevist, Dotarem, etc...): paramagnetic
  - Iron oxide (Feridex): superparamagnetic
  - Manganese (Mn-DPDP): paramagnetic
- Paramagnetic contrast agents are primarily used as  $T_1$ -shortening agents => **signal enhancement on  $T_1$ -weighted images**
- Superparamagnetic contrast agents are primarily used as  $T_2/T_2^*$ -shortening agents => **signal drop/void on  $T_2$ -weighted images**



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## CNR: Contrast Agents Theory

- Effect of contrast agent on tissue relaxation times is best described using relaxation rates:  $R_1=1/T_1$ ,  $R_2=1/T_2$
- Relaxation rates are additive
- In the presence of contrast agent, the new relaxation rate is:

$$R' = R + rC = 1/T' + rC$$

$R'$  is the relaxation rate in the presence of contrast agent

$R$  is the original relaxation rate (e.g., of tissue, water, etc...)

$C$  is the concentration of contrast in tissue, in mM (mMolar = mmol/L)

$r$  is **specific relaxivity** of the contrast agent, in mM/s (4mM/s for Gd)



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## CNR: Contrast Agents Theory Cont.

- Example:
  - We would like to create a 50 ml phantom with  $T_1=200\text{ms}$
  - We have 5 ml of Dotarem, with concentration of 500mM
  - The relaxivity of Dotarem is 4/mMs.
  - The  $T_1$  of pure water at 7T is around 3sec.
- We, first compute the concentration of solution:

$$C = \frac{R_1' - R_1}{r_1} = \frac{(1/0.2 - 1/3)/s}{4/mMs} = 1.167\text{mM}$$

- Then, we compute the volume of contrast agent we need:

$$C_{sol} V_{sol} = C_{Gd} V_{Gd} \Rightarrow V_{Gd} = \frac{C_{sol} V_{sol}}{C_{Gd}}$$

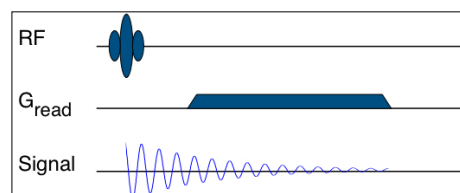
$$V_{Gd} = \frac{1.167 * 50}{500} \text{mM} = 0.117\text{ml} = 117\mu\text{l}$$



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## Pulse Sequence Diagrams

- Is a simple means of showing how the RF (excitation) and gradient pulses (spatial encoding) are applied
- Horizontal axis = time, vertical axis = amplitude
- From the sequence diagram we can get the following info:
  - Timing parameters: TE, TR, diffusion time, etc
  - RF parameters: shape, flip angle  $\alpha$ .
  - Gradient parameters: strength and duration
  - Knowledge of how we transverse the  $k$ -space



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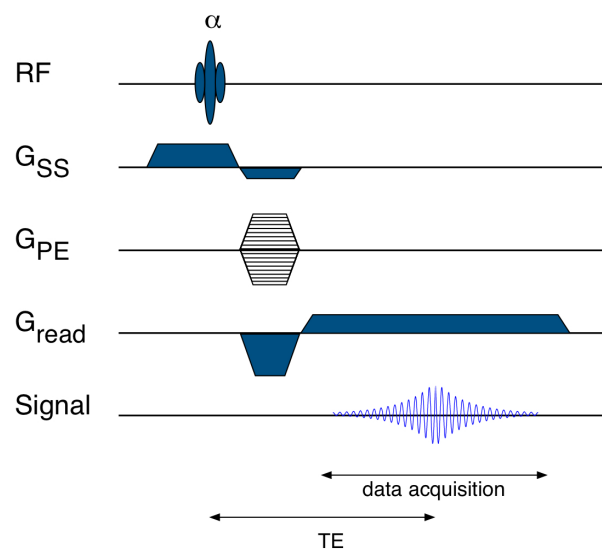
## Gradient Echo Sequence or GRE

- Echo is formed by de-phasing and re-phasing of an MR signal by an imaging gradient => **gradient echo**
- Effect of magnet inhomogeneities and local susceptibility changes are NOT compensated ( $T_2^*$  decay)
- Can give  $PD$ ,  $T_1$ ,  $T_2^*$  contrast (in special cases also  $T_2$ )
- RF pulse ( $\alpha$ ) can be any value between  $0^\circ$  and  $90^\circ$
- Speed is achieved by using a small flip angle and short  $TR$
- Three main groups of gradient echo sequences:
  - **Spoiled or incoherent** GE (e.g., FLASH)
  - **Rewound or coherent** GE (e.g., FISP)
  - **Steady state/contrast enhanced** (e.g., SSFP)
- Ideally suited for studies in which speed is important: dynamic contrast MRI, angiography, breath-hold studies and 3D imaging (3D FT).



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## GRE: Sequence Diagram



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## Fast Low Angle SHot or FLASH ( $T_1 \gg TR$ )

- The steady-state MR signal in FLASH is:

$$S_{MRI} = \rho \frac{\sin \alpha \cdot \left(1 - e^{-\frac{TR}{T_1}}\right) \cdot e^{-\frac{TE}{T_2^*}}}{1 - \cos \alpha \cdot e^{-\frac{TR}{T_1}}}$$

- Flip angle  $\alpha$  also determines image contrast
- For each value of  $T_1$  there is an optimum flip angle at which MR signal will be at its maximum => **Ernst angle**

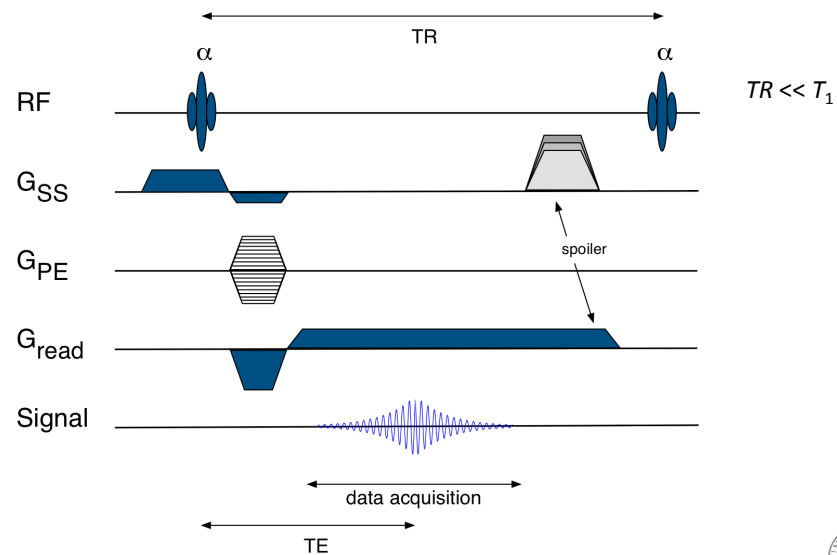
$$\alpha_{Ernst} = \cos^{-1} \left( e^{-\frac{TR}{T_1}} \right)$$

- For  $\alpha < \text{Ernst angle}$  => **PD weighting**
- For  $\alpha > \text{Ernst angle}$  =>  **$T_1$  weighting**



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## FLASH: Sequence Diagram



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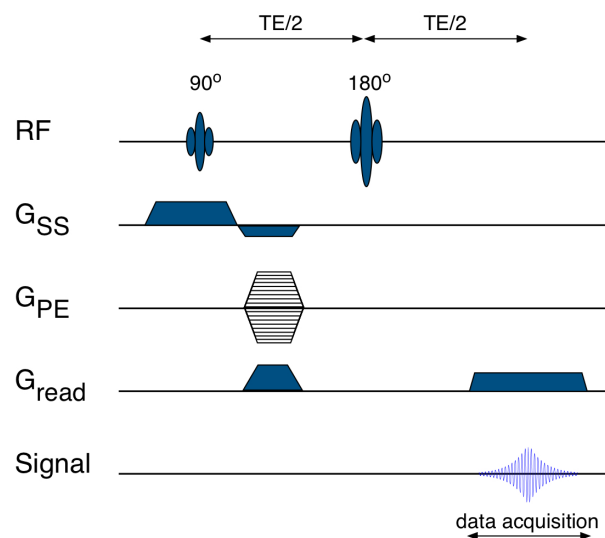
## Spin Echo Sequence or SPE

- Echo is formed by a  $180^\circ$  pulse => **spin echo**
- Effect of magnet inhomogeneities and local susceptibility changes are compensated ( $T_2$  decay)
- Can give  $PD$ ,  $T_1$ ,  $T_2$  contrast
- RF pulse ( $\alpha$ ) is a  $90^\circ$  pulse
- Speed is achieved by using multiple echoes to collect several lines of k-space in a single shot (within  $TR$  period) => segmentation (fast or turbo SE)
- Two main groups of spin echo sequences:
  - **Inversion recovery SE** (e.g., FLAIR)
  - **Fast or Turbo SE** (e.g., RARE, MSME)
- Ideally suited for studies in which susceptibility effects are big: near air/tissue interfaces in lungs, near bone/tissue interfaces to study joints...



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## SPE: Sequence Diagram



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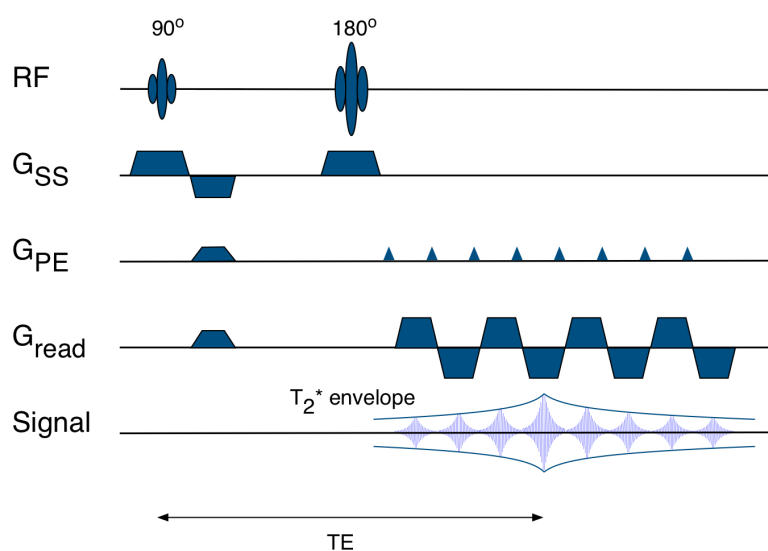
## Echo Planar Imaging EPI (SE-EPI or GE-EPI)

- The fastest pulse sequence available => the entire image can be collected in less than 100 ms
- Two main groups of EPI sequences:
  - **Spin-echo** EPI
  - **Gradient echo** EPI
- Can be **single-shot** or **multi-shot**
- In single-shot case, the whole of  $k$ -space is sampled with gradient echoes under a single spin echo (in SE-EPI) or under an FID (in GE-EPI)
- Ideally suited for studies in which speed is important: dynamic, diffusion-weighted imaging (EPI-DTI) and fMRI.



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## EPI: sequence diagram for SE-EPI



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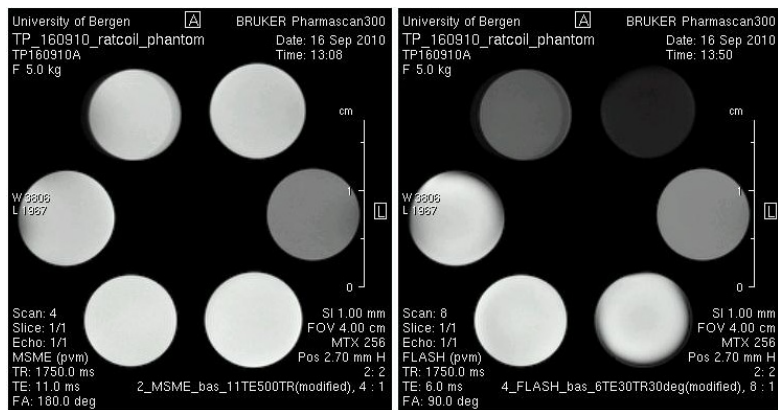


## Some Examples



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## PD-Weighting: MSME vs. FLASH at long TR



**MSME; PD +  $T_2$  weighting**

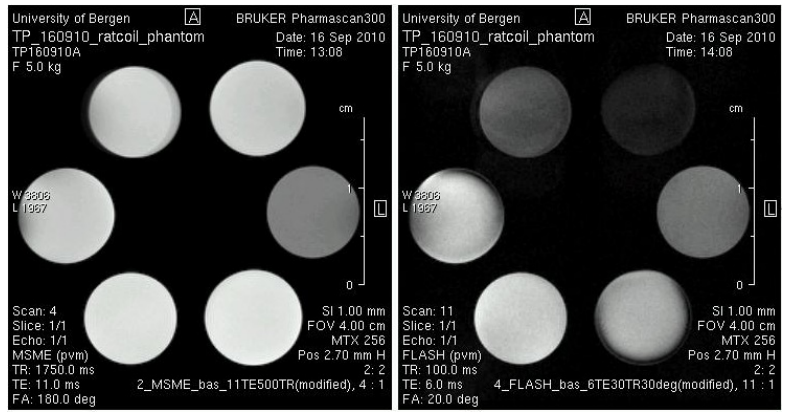
**FLASH, PD +  $T_2^*$  weighting**

Observe the contrast in the two images. Where do you see the main difference? Why? Hint: think of  $T_2^*$  and chemical shift.



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### PD-Weighting: MSME vs. FLASH at short TR, small $\alpha$



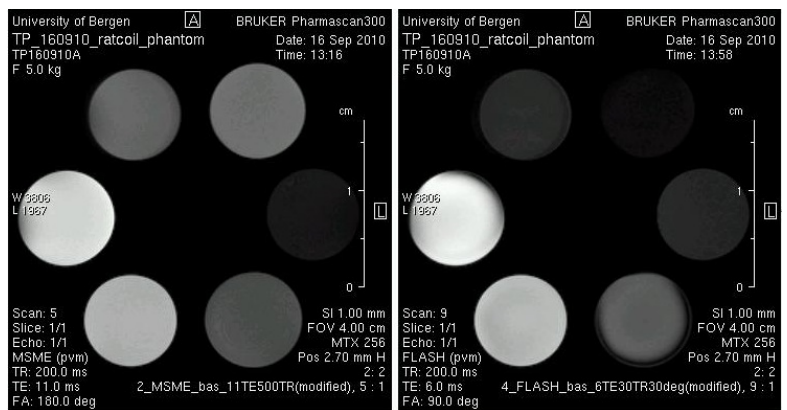
**MSME; PD + T<sub>2</sub> weighting**

**FLASH, PD + T<sub>2</sub>\* weighting**

Observe the contrast in the these images as compared to the previous two. Why is the SNR of the right image so much worse now? Hint: think about TR and the total scanning time.



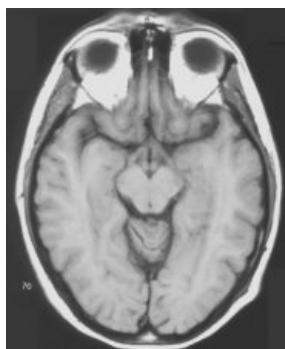
### T<sub>1</sub>-Weighting: MSME vs. FLASH at short TR, large $\alpha$



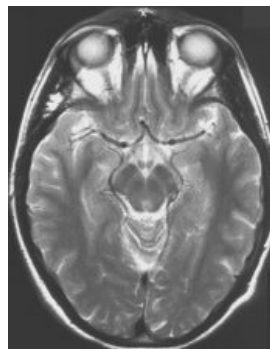
Observe the contrast in the these two images. Again, where do you see the main difference? Why?



## $T_1$ and $T_2$ Weighted Images, Comparison



**T1 weighted image**  
short TR, short TE  
"Free water is black"



**T2 weighted image**  
long TR, long TE  
"Free water is white"

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## Section Summary: Choice of TR and TE for SE Sequences

TR	TE	TE
	Short	Long
Short	$T_1$ -wt	--
Long	PD-wt	$T_2$ -wt

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## Section Summary: Choice of TE and $\alpha$ for GE Sequences with short TR

$\alpha$ (flip angle)	TE	TE
	Short	Long
Small	PD-wt	$T_2^*$ -wt
Large	$T_1$ -wt	--



## Which Sequence is Right for My Application?

- $T_1$ -weighted sequences:
  - Anatomy
  - When using a  $T_1$  contrast (DCE-MRI)
  - Fat imaging
- $T_2$ -weighted sequences:
  - Pathology (tumors, edema, etc)



## Optimizing Pulse Sequence Parameters

